

Classwork 13: Trend Stationary Processes

EC 421

2024-05-21

1) Show that y_t is nonstationary when $y_t = \beta_0 + \beta_1 t + u_t$, where $u_t \sim \text{iid } N(0, \sigma^2)$.

2) Suppose x_t and y_t are unrelated except that they both have time trends, so

$$y_t = \alpha_0 + \alpha_1 t + w_t$$

$$x_t = \gamma_0 + \gamma_1 t + v_t$$

Where w_t and v_t are iid $N(0, 1)$. If we estimate the model $y_t = \beta_0 + \beta_1 x_t + u_t$, why do we often conclude that $\beta_1 \neq 0$? What will the sign of $\hat{\beta}_1$ be?

3) In the previous problem, should we expect that as the number of observations t increases, we find that x seems to have an effect on y less often?

Make a hypothesis and then answer the question by doing a monte carlo simulation in R using `map` or `map_dfr`. By looking at your results, do the estimates from this model seem to be biased or inconsistent?

Hint: I would solve this problem like this: generate a dataset with variables t , x , and y . t should be the sequence $1:n$, where n is the sample size (which you will end up varying). x should be some linear function of t and random noise. y should be another linear function of t and random noise. You will take that dataset and use `lm()` to estimate the model $y \sim x$, then select the estimate for beta 1. Write a function that takes a sample size n and does everything I just talked about, returning n and the estimate for beta 1. That's the `.f` you'll use in your `map_dfr` simulation. The `.x` should be sample sizes you want to test: something like a vector of a bunch of 5s, 10s, 20s, 40s, etc. I would present my final results using `geom_density` with `fill` represented by n .